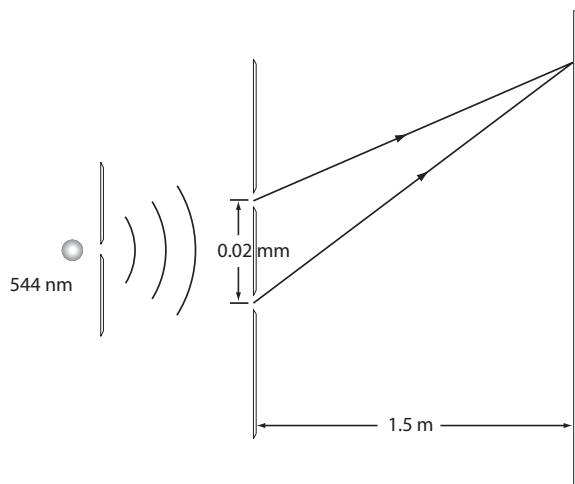


Wave Optics Practice Items

1. Light has the property of being able to bend around corners. This phenomenon is known as
- diffraction
 - refraction
 - dispersion
 - polarization

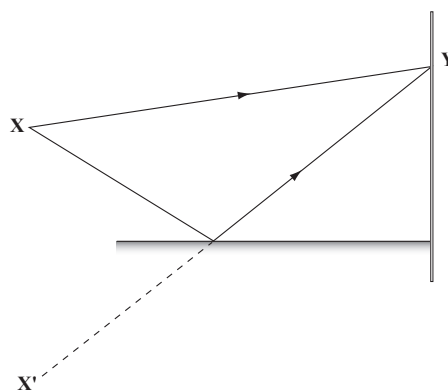
2. The figure below shows light from a helium-neon laser passing through two slits before striking a screen. Compared to the light from the upper slit, how much further does the light from the lower slit travel to reach a point on the screen at an angle 30° above the two slits?

- 2.7×10^{-7} m
- 1.0×10^{-5} m
- 7.5×10^{-5} m
- 7.5×10^{-1} m



3. A light source is placed at point **X** near a mirror as shown in the figure below. Light rays of wavelength λ can reach the screen either by a direct path or through reflection. An interference pattern is observed on the screen similar to the pattern observed in Young's interference. Which of the following describes the condition for a *dark* fringe at point **Y**?

- $|X'Y| - |XY| = n\lambda \quad (n = 1, 2, 3 \dots)$
- $|X'Y| - |XY| = (n + \frac{1}{2})\lambda \quad (n = 1, 2, 3 \dots)$
- $|X'Y| - |XY| = n\lambda \quad (n = 1, 3, 5 \dots)$
- $|XX'|^2 + |XY|^2 = |X'Y|^2$



4. What is the minimum thickness of a soap bubble where constructive interference occurs when illuminated by a 589 nm sodium lamp?
- 147 nm
 - 295 nm
 - 589 nm
 - 1.18 μm
5. A coin is suspended halfway between a monochromatic light source and a screen. Circular fringes are observed near the shadow's edge. What is observed in the center of the shadow?
- an inverted image of the coin
 - an iridescent circular pattern
 - a cross-hatch pattern of bright fringes
 - a bright spot

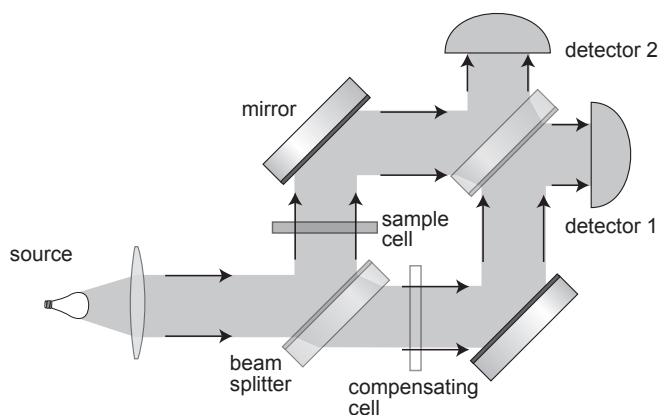
6. What would happen if the monochromatic light source in Young's double slit experiment were replaced with white light?
- No diffraction would occur.
 - The central fringe would be violet and the outermost fringes would be red.
 - A more widely spaced pattern of white fringes would appear.
 - The bright central fringe would be white and the other fringes would be colored.
7. Approximately $50\ \mu\text{m}$ is the minimum separation between two point sources the normal human eye can distinguish at the near point. This is approximately equal to the thickness of a human hair. Why can't object points nearer than $50\ \mu\text{m}$ from each other be distinguished by the human eye?
- The inverted real image would land behind the retina.
 - Too many orders of diffracted light would be captured to separate the object points.
 - The two points could be distinguished if moved further away than the near point.
 - The central maxima of the airy disk images of the two object points would overlap.
8. The first diffraction order was observed at a 30° angle to the surface when incident X-rays having a wavelength of $2.65 \times 10^{-10}\ \text{m}$ were reflected off of the surface of a NiS crystal. The reflected rays were visualized photographically. What is the spacing between atomic layers in this crystal?
- $1.33\ \text{\AA}$
 - $2.65\ \text{\AA}$
 - $3.75\ \text{\AA}$
 - $5.30\ \text{\AA}$
9. If one places a block of a birefringent material such as calcite onto a sheet of paper with an image, one sees two images through the block. If the two images are then viewed through a rotating sheet of polaroid film, the two images
- alternately appear and disappear.
 - merge into a single image.
 - will be inverted.
 - will be magnified.
10. Transmission of plane polarized light through a solution of pure optical isomer results in rotation of the optical axis of the transmitted light. The degree of observed rotation may be measured by a polarimeter. The rotation in degrees observed upon passing polarized light through a path length of 1 decimeter (dm) at a concentration of 1 g/mL is known as the
- circular birefringence
 - dextrarotation
 - specific rotation
 - chirality
11. UV circular dichroism spectroscopy is primarily used within life sciences research to investigate
- the secondary structure of proteins.
 - the kinetics of enzymatic reactions.
 - the crystal field splitting energy of metallic cofactors.
 - the UV absorbance of biological pigments.

The following passage pertains to questions 12 - 16.

The Mach–Zehnder interferometer is used to determine the relative phase shift variations between two collimated beams derived by splitting light from a single source. The interferometer has been used, among other things, to measure phase shifts between the two beams caused by a change in the optical path length of one of the beams by the introduction of a sample.

A collimated beam is split by a half-silvered mirror. The two resulting beams (the “sample beam” and the “reference beam”) are each reflected by a mirror. The two beams then pass a second half-silvered mirror and enter two detectors. Phase change occurs for a reflection when a wave reflects off a boundary from low to high refractive index but not when it reflects off a boundary from high to low.

The fully silvered and half-silvered surfaces of all mirrors, except the last, face the inbound beam, and the half-silvered surface of the last mirror faces the outbound beam exiting in the same orientation as the collimated original beams.



The Mach–Zehnder interferometer is a more versatile instrument than the Michelson interferometer. Each of the well separated light paths is traversed only once, and the fringes can be adjusted so that they are localized in any desired plane. Typically, the fringes would be adjusted to lie in the same plane as the test object, so that fringes and test object can be photographed together.

12. The Mach–Zehnder interferometer works because when two waves originating from a single source recombine a pattern results determined by
- A. the difference in frequency between the waves
 - B. the phase difference between the waves
 - C. the refractive index of the beam splitter
 - D. the difference in wavelength between the waves
13. Light traveling in test and reference beams of equal optical path through a Mach–Zehnder interferometer leads to which result on detector 2?
- A. a bright pattern
 - B. no image
 - C. incoherence in the transversal direction
 - D. a horizontally inverted image
14. A sample is introduced into the sample cell in which heat transfer and convection currents produce varying indices of refraction throughout the sample.
- A. A fringe pattern appears on both detectors.
 - B. No results may be recorded.
 - C. Dispersion of the monochromatic source occurs.
 - D. Detector 2 receives polarized light.

15. What is a likely result with a white light source with an empty sample cell if the compensating cell is not also included?
- A. fringes of varying color on detector 1
 - B. fringes of varying color on detector 2
 - C. fringes of varying color on both detectors
 - D. no interference patterns
16. A Mach-Zehnder interferometer is illuminated by light of $\lambda_{\text{vacuum}} = 500 \text{ nm}$ ($\tilde{\nu} = 20,000 \text{ cm}^{-1}$). The interferometer contains a 1 cm gas-filled sample cell. As the gas is evacuated from the cell, 8 fringes cross a point in the field of view of detector 1. The refractive index of the gas at its original concentration is closest to which of the following values?
- A. 1.04
 - B. 1.004
 - C. 1.0004
 - D. 1.00004
-

Wave Optics

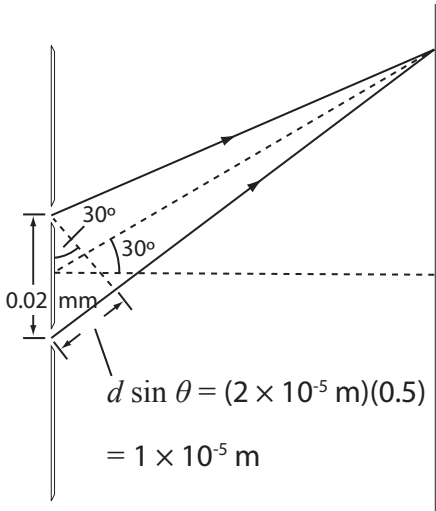
Answers and Explanations

1. A

Diffraction is the bending of waves around the corners of an obstacle or through an aperture into the region of geometrical shadow of the obstacle. The diffracting object or aperture effectively becomes a new source of the propagating wave. Diffraction can be understood in terms of the Huygens principle that treats each point in a propagating wave-front as a collection of individual spherical wavelets. The characteristic interference pattern resulting from diffraction is most pronounced when light from a coherent, monochromatic source (such as a laser) encounters a slit/aperture that is comparable in size to its wavelength.

2. B

The extra distance from the lower slit is the product of the spacing between the two slits, d , and the sine of the angle, θ , to the point on the screen mentioned in the passage.

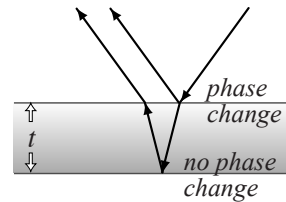


3. B

$|X'Y| - |XY|$ equals the extra distance traveled by the reflected ray. One might think that a bright fringe occurs if this extra distance is an integral number of wavelengths ($n\lambda$), but remember that when light reflects within a fast medium off of a high index of refraction surface it undergoes a 180° phase change, so we need to offset the condition for constructive interference by half a wavelength.

4. A

In thin film interference, light reflected from the front and rear surfaces of a thin film combines to form a resultant wave. Whether constructive or destructive interference occurs depends on whether the combining rays are in or out of phase. The phase difference of the rays depends on the wavelength of light in the film medium, the thickness of the film (assume the light rays are nearly normal to the surface), and whether or not there are any phase changes with either reflection. Hard reflection is reflection off of a medium of higher index of refraction and leads to a 180° change of phase. Soft reflection is reflection off of a medium of lower index of refraction and does not produce a change of phase.



Normally, in interference problems, a path difference ($2t$ with thin films) equal to an integral number of wavelengths produces constructive interference, but if one of the reflections is hard and the other soft the result is destructive interference.

Condition of Constructive Interference
(with one reflection having a phase change)

$$2t = \left(m + \frac{1}{2}\right) \lambda_n$$

($m = 0, 1, 2, \dots$)

In other words, if the thickness of the soap film is one fourth the wavelength of the incident light, 147nm , the path difference would be half the wavelength. Because one of the reflections resulted in a 180° change of phase, this produces constructive interference.

5. D

Diffraction leads to bending of the light around the coin into the region of its shadow. The edges of the coin effectively becomes a new source of the propagating light. The diffracting rays from different points along the entire edge circumference will have traveled exactly the same distance to the very center of the coin, so they will be in phase there and produce a bright spot resulting from constructive interference.

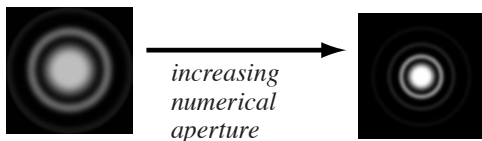
6. D

Because there is no path difference from either slit to the position of the central fringe, all of the variously colored components of white light will be in phase in the center. Elsewhere on the screen, however, the phase difference of the light rays from the two slits will depend on the wavelength, so at a certain angle only a certain wavelength will be in phase while others will be undergoing destructive interference.

7. D

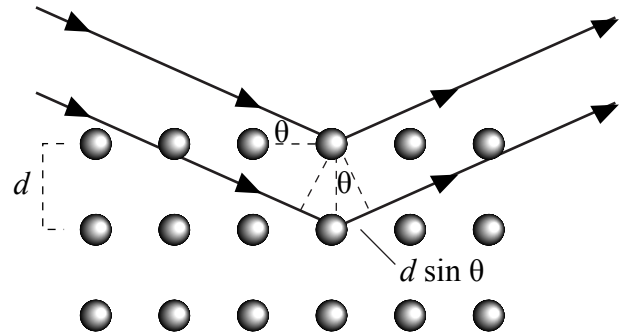
Diffraction of light passing through a circular aperture produces an interference pattern similar to single slit diffraction. By Huygen's principle, each portion of the aperture acts as a source of waves. For a given image point, the interference of wavelets yields a diffraction pattern known as an airy disk. Widening the slit narrows the central maximum in single slit diffraction. Likewise, widening a circular aperture increases the phase difference possible for different light paths, increasing the number of diffraction orders captured, which decreases the size of the central maxima of the airy disk image of a given point source.

When the central maximum of one airy disk falls on the first minimum of another (Rayleigh's criterion), the images are said to be just resolved. If the width of the pupil were greater, the human eye could resolve finer detail. This would increase the number of diffraction orders captured and decrease the size of the central maxima of object point airy disc patterns. Decreasing the size of central maxima increases the ability to resolve two airy disk patterns.



8. B

The basic principles underlying X-ray crystallography are similar to thin film interference. It can be seen in the figure below that the path length difference for light reflecting off of the top layer of the crystal and the adjacent layer below it is $2d \sin \theta$.



Bragg's Law describes how constructive interference will be observed if this path length difference is equal to an integral number of wavelengths of the incident light.

$$2d \sin \theta = n\lambda \quad (n = 1, 2, 3 \dots)$$

The first diffraction order would at an incident angle of 30° if the crystal layer spacing exactly equaled the wavelength of the incident X-rays.

$$2d \sin 30^\circ = (1) \lambda$$

$$d = \lambda$$

9. A

In birefringent materials, such as calcite and quartz, the index of refraction is not the same in all directions. Double refraction causes an unpolarized light beam to be split into an ordinary (O) ray and an extraordinary (E) ray, which are polarized in mutually perpendicular directions. The two images seen when the block is placed on the paper are produced by these two rays respectively.

A polaroid film only allows the components of the electric field vibrations to pass that are parallel to its transmission axis. Because the ordinary and extraordinary rays are polarized in mutually perpendicular directions, the rotating polaroid film will allow a varying intensity of transmission of each which is phase shifted in the rotation. In other words, the two images will alternately appear and disappear.

10. C

Specific rotation is common standard for optical rotation. It allows us to compare samples collected under different concentrations and path lengths.

$$[\alpha] = \frac{\alpha_{\text{observed}}}{c \times l}$$

Diagram illustrating the formula for specific rotation $[\alpha]$. The formula is $[\alpha] = \frac{\alpha_{\text{observed}}}{c \times l}$. Arrows point from the following labels to the corresponding parts of the formula: "observed rotation" points to α_{observed} ; "specific rotation" points to $[\alpha]$; "concentration g/ml" points to c ; and "path length dm" points to l .

11. A

Circular dichroism spectroscopy is based on the differential absorption of left-hand and right-hand circular polarized light. Circularly polarized light occurs when the direction of the electric field vector rotates about its propagation direction. At a single point in space, the circularly polarized-vector will trace out a circle over one period of the wave frequency.

The far-UV CD spectrum of a protein can reveal information about the secondary structure of the protein. The technique can be used to estimate the fraction of the protein in the alpha-helix or beta-sheet conformations, for example.

12. B

A basic scenario repeats itself throughout wave optics from Young's interference, thin layer interference, to the Michelson or Mach-Zehnder interferometers. Light which was originally in phase and traveling together is separated in some way, whether by diffracting through separate slits (or different points in the same aperture in single slit diffraction), reflecting off different boundaries in a thin layer, or being split by a beam splitter to travel different paths in interferometry. The rays then recombine. Interference results. The different optical paths they have followed may or may not have produced a phase difference leading to either constructive or destructive interference.

13. B

At detector 2, in the absence of a sample, the sample beams and reference beams will arrive with a phase difference of half a wavelength, yielding complete destructive interference. When light traveling in a fast medium reflects off a boundary to a slow medium, the light undergoes a 180° phase shift. This is known as a hard reflection. The reference beams arriving at detector 2 will have undergone a 180° phase shift of due to one hard reflection. The sample beams arriving at detector 2 will have undergone two hard reflections. Therefore, when there is no sample, only detector 1 receives light.

14. A

An alteration of optical path occurs as the collimated sample beams travel through the sample. The collimated beams are variously altered across the wave front. When they recombine with the reference beam, the phase shift differences create an image of the sample as an interference pattern on both detectors. Because both the sample and reference beams on their paths to detector 1 undergo two hard reflections, while on their paths to detector 2 undergo two and one hard reflections respectively, there is a 180° offset in the phase shift relationships reflected in the images on the two detectors, so they will appear as negative images of each other.

15. C

The collimated beams of white light passing through the glass of the sample cell will have undergone dispersion. Dispersion occurs in glass because the phase velocity of light in glass varies slightly with the frequency of light, ie. the index of refraction in glass is slightly different for the different colors. Without the compensating cell present in the path of the reference beam, the dispersion occurring in the sample cell will cause the optical path of the sample beam to slightly different for each frequency. This will lead to a pattern of colored fringes in each detect

16. C

As the gas is being evacuated from the sample cell, the index of refraction within is steadily decreasing from the value for the gas at its original concentration to the vacuum value of 1. As the index of refraction decreases, the wavelength of the light within the sample cell increases. For light of a given frequency, the faster the medium the lower the index of refraction and the longer the wavelength.

$$\frac{v_2}{v_1} = \frac{n_1}{n_2} \quad \frac{\lambda_2}{\lambda_1} = \frac{v_2}{v_1} \quad \frac{\lambda_2}{\lambda_1} = \frac{n_1}{n_2}$$

As the wavelength in the sample cell increases, eight phase shift cycles occur in the interference of the sample and reference beams. In other words, it required eight more wavelengths to cross the sample cell containing the gas than the vacuum. Those eight extra wavelengths are subtracting from the optical path of the sample beam as the sample cell is being evacuated.

A helpful clue in the question stem might make the problem easier to conceptualize and solve. In addition to presenting the wavelength in nm, it also provides the same value in the form of wavenumber, $\tilde{\nu}$. The wavenumber is the reciprocal of the wavelength. A value of $20,000 \text{ cm}^{-1}$ tells you that there are 20,000 cycles per centimeter for this particular frequency of light in a vacuum. The sample cell itself is 1 cm long. The wavenumber of the light in the gas was therefore $20,008 \text{ cm}^{-1}$. Because wavenumber is the reciprocal of the wavelength, which is inversely proportional to the index of refraction, wavenumber is directly proportional to index of refraction.

$$\frac{n_{\text{gas}}}{n_{\text{vacuum}}} = \frac{2.0008 \times 10^4 \text{ cm}^{-1}}{2.0 \times 10^4 \text{ cm}^{-1}}$$

$$\frac{n_{\text{gas}}}{1} = \frac{2.0 \times 10^4 + 8}{2.0 \times 10^4}$$

$$n_{\text{gas}} = 1 + \frac{8}{2.0 \times 10^4}$$

$$n_{\text{gas}} = 1 + 4.0 \times 10^{-4} = 1.0004$$

